# APRIORI ALGORITHM

### **Motivation: Association Rule Mining**

 Given a set of transactions, find rules that will predict the occurrence of an item based on the occurrences of other items in the transaction

#### **Market-Basket transactions**

TID	Items
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke

#### **Example of Association Rules**

 $\{Diaper\} \rightarrow \{Beer\},\$  $\{Milk, Bread\} \rightarrow \{Eggs, Coke\},\$  $\{Beer, Bread\} \rightarrow \{Milk\},\$ 

### **Applications: Association Rule Mining**

- \* ⇒ Maintenance Agreement
  - What the store should do to boost Maintenance Agreement sales
- Home Electronics  $\Rightarrow$  \*
  - What other products should the store stocks up?
- Attached mailing in direct marketing
- Detecting "ping-ponging" of patients
- Marketing and Sales Promotion
- Supermarket shelf management

### **Definition: Frequent Itemset**

#### Itemset

- A collection of one or more items
  - •Example: {Milk, Bread, Diaper}
- k-itemset
  - •An itemset that contains k items
- Support count (σ)
  - Frequency of occurrence of an itemset
  - E.g.  $\sigma(\{Milk, Bread, Diaper\}) = 2$
- Support
  - Fraction of transactions that contain an itemset
  - E.g. s({Milk, Bread, Diaper}) = 2/5

#### Frequent Itemset

 An itemset whose support is greater than or equal to a *minsup* threshold

TID	Items
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
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### **Definition: Association Rule**

#### Association Rule

- An implication expression of the form  $X \rightarrow Y$ , where X and Y are itemsets
- Example: {Milk, Diaper}  $\rightarrow$  {Beer}
- Rule Evaluation Metrics
  - Support (s)

•Fraction of transactions that contain both X and Y

- Confidence (c)

•Measures how often items in Y appear in transactions that contain X

TID	Items
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
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Example:







### **Association Rule Mining Task**

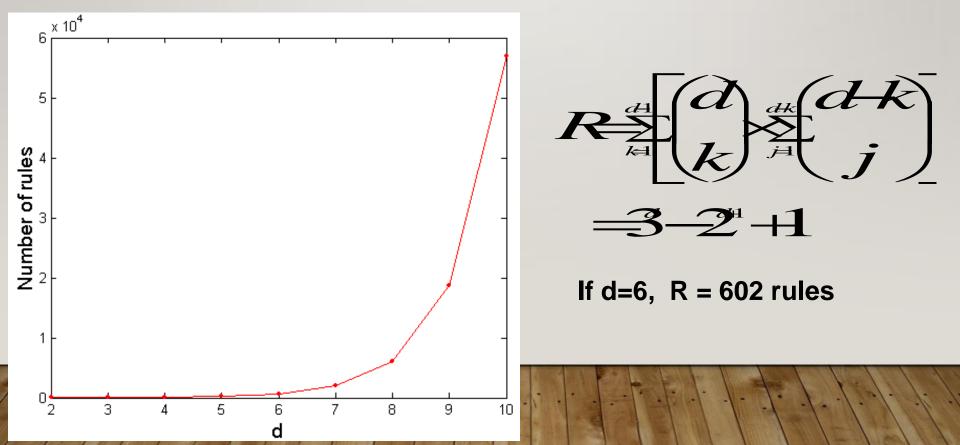
- Given a set of transactions T, the goal of association rule mining is to find all rules having
  - support ≥ minsup threshold
  - confidence ≥ minconf threshold

### Brute-force approach:

- List all possible association rules
- Compute the support and confidence for each rule
- Prune rules that fail the *minsup* and *minconf* thresholds
- ⇒ Computationally prohibitive!

### **Computational Complexity**

- Given d unique items:
  - Total number of itemsets = 2<sup>d</sup>
  - Total number of possible association rules:



## Mining Association Rules: Decoupling

TID	Items
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke

#### Observations:

#### Example of Rules:

 $\{ Milk, Diaper \} \rightarrow \{ Beer \} (s=0.4, c=0.67) \\ \{ Milk, Beer \} \rightarrow \{ Diaper \} (s=0.4, c=1.0) \\ \{ Diaper, Beer \} \rightarrow \{ Milk \} (s=0.4, c=0.67) \\ \{ Beer \} \rightarrow \{ Milk, Diaper \} (s=0.4, c=0.67) \\ \{ Diaper \} \rightarrow \{ Milk, Beer \} (s=0.4, c=0.5) \\ \{ Milk \} \rightarrow \{ Diaper, Beer \} (s=0.4, c=0.5)$ 

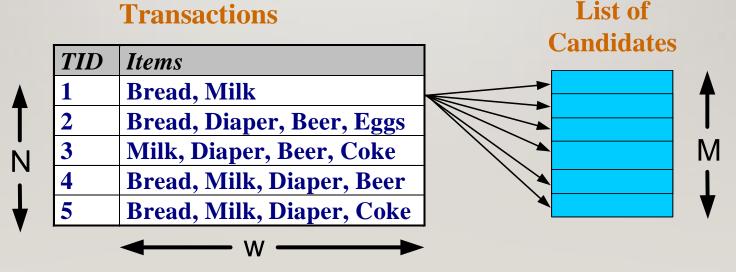
- All the above rules are binary partitions of the same itemset: {Milk, Diaper, Beer}
- Rules originating from the same itemset have identical support but can have different confidence
- Thus, we may decouple the support and confidence requirements

### **Mining Association Rules**

- Two-step approach:
  - 1. Frequent Itemset Generation
    - Generate all itemsets whose support ≥ minsup
  - 2. Rule Generation
    - Generate high confidence rules from each frequent itemset, where each rule is a binary partitioning of a frequent itemset
- Frequent itemset generation is still computationally expensive

### **Frequent Itemset Generation**

- Brute-force approach:
  - Each itemset in the lattice is a candidate frequent itemset
  - Count the support of each candidate by scanning the database



Match each transaction against every candidate

Complexity ~ O(NMw) => Expensive since M = 2

### **Reducing Number of Candidates: Apriori**

• Apriori principle:

is is known as the

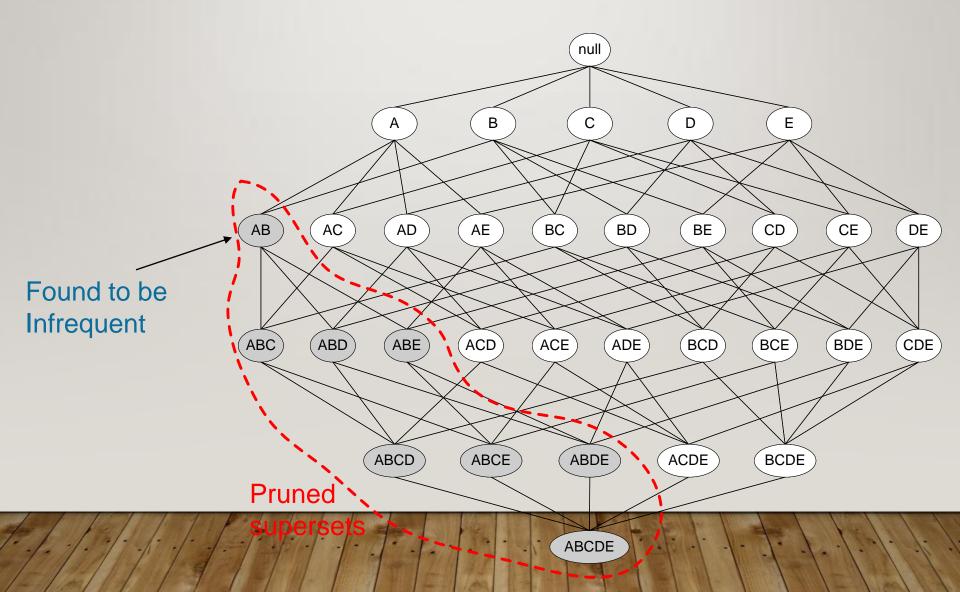
- If an itemset is frequent, then all of its subsets must also be frequent
- Apriori principle holds due to the following property of the support measure:



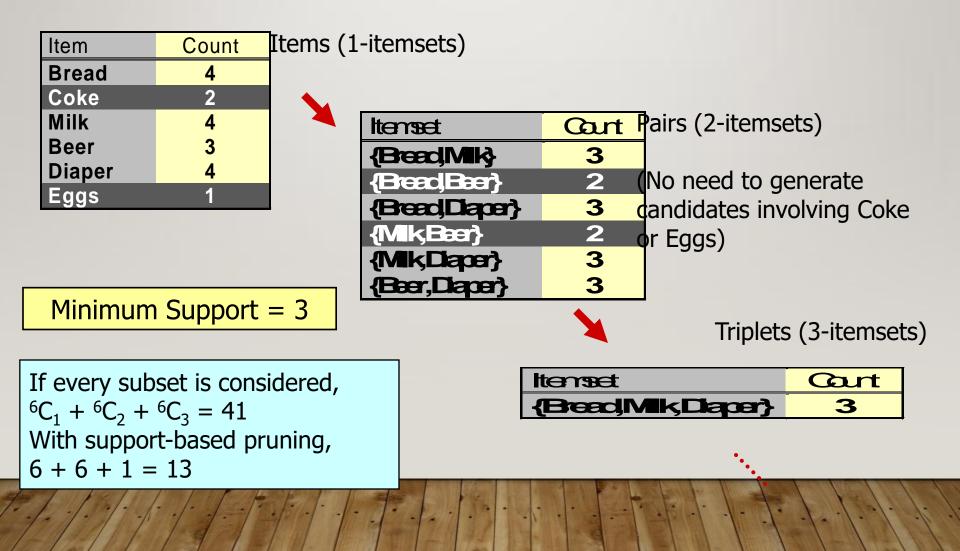
Support of an itemset never exceeds the support of its subsets

property of support

### **Illustrating Apriori Principle**



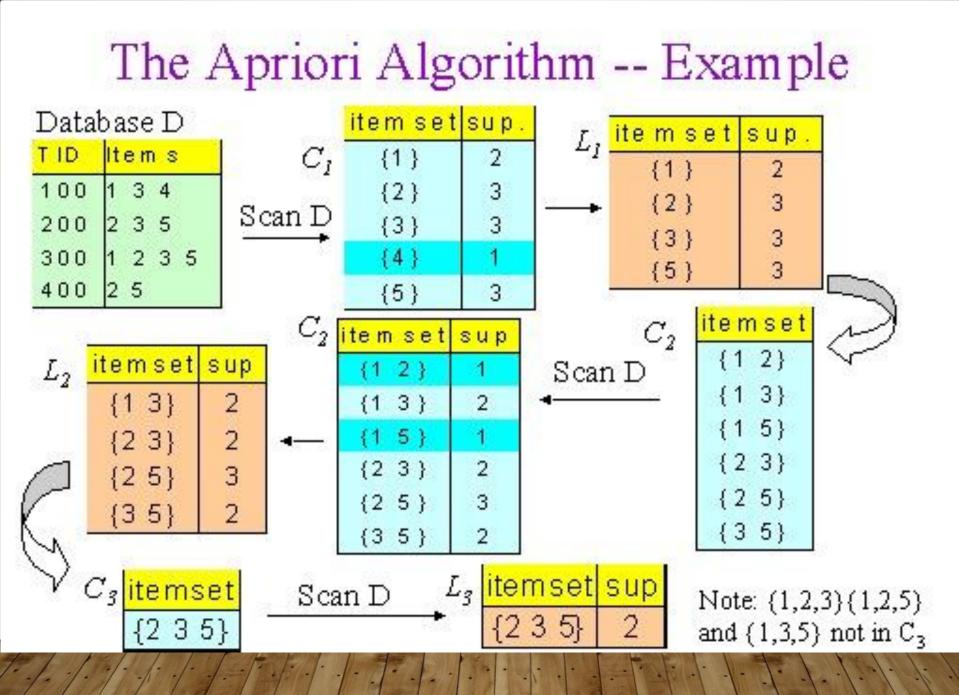
### **Illustrating Apriori Principle**



# The Apriori Algorithm

 $C_k$ : Candidate itemset of size k  $L_k$ : frequent itemset of size k

 $L_{I} = \{ \text{frequent items} \}; \\ \text{for } (k = 1; L_{k} != \emptyset; k ++) \text{ do begin} \\ C_{k+I} = \text{candidates generated from } L_{k}; \\ \text{for each transaction } t \text{ in database do} \\ \text{ increment the count of all candidates in } \\ C_{k+I} \text{ that are contained in } t \\ L_{k+I} = \text{candidates in } C_{k+I} \text{ with min_support } \\ \text{end} \\ \text{return } \cup_{k} L_{k}; \end{cases}$ 

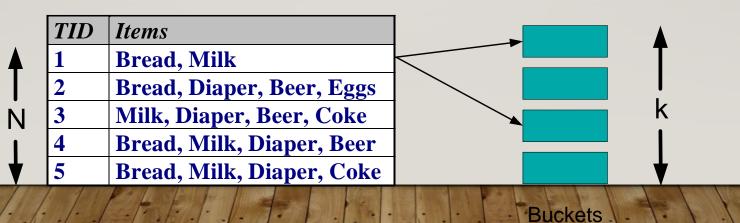


### **Apriori: Reducing Number of Comparisons**

- Candidate counting:
  - Scan the database of transactions to determine the support of each candidate itemset
  - To reduce the number of comparisons, store the candidates in a hash structure
    - Instead of matching each transaction against every candidate, match it against candidates contained in the hashed buckets

#### **Transactions**





### **Apriori: Implementation Using Hash Tree**

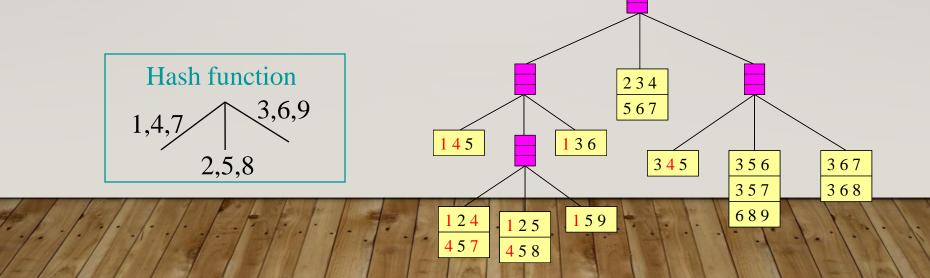
Suppose you have 15 candidate itemsets of length 3:

 $\{1\ 4\ 5\},\ \{1\ 2\ 4\},\ \{4\ 5\ 7\},\ \{1\ 2\ 5\},\ \{4\ 5\ 8\},\ \{1\ 5\ 9\},\ \{1\ 3\ 6\},\ \{2\ 3\ 4\},\ \{5\ 6\ 7\},\ \{3\ 4\ 5\},\ \{3\ 5\ 6\},\ \{3\ 5\ 7\},\ \{6\ 8\ 9\},\ \{3\ 6\ 7\},\ \{3\ 6\ 8\} \}$ 

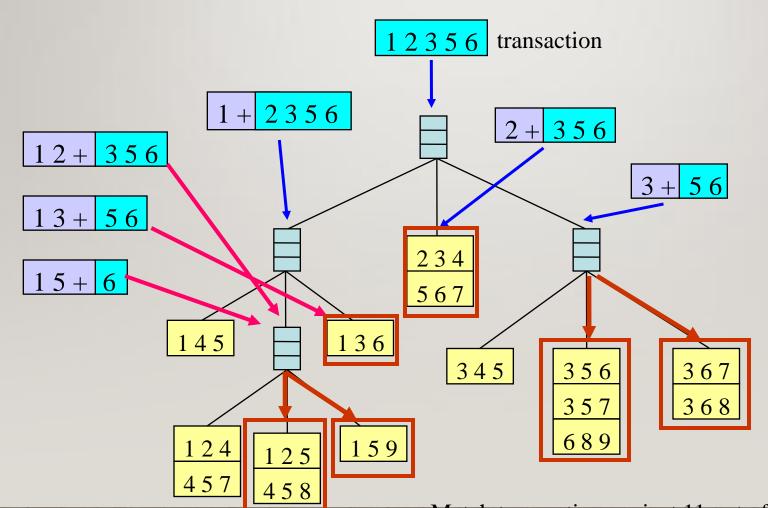
You need:

- Hash function
- Max leaf size: max number of itemsets stored in a leaf node

(if number of candidate itemsets exceeds max leaf size, split the node)



### **Apriori: Implementation Using Hash Tree**



Match transaction against 11 out of 15 candidates

### **REFERENCES** :

• Fast algorithms for mining association rules in large databases